

1 The region of feasible solutions has an important property called -

- A. The concave property
- B. The convex property
- C. The bounded property
- D. The shaded property

2 Which is FALSE?

- A. $\frac{1}{r} = \cos\theta + 2\sin\theta + 3$ represents a conic
- B. $\frac{1}{r} = 4$ represents a circle
- C. $\frac{1}{r} = 2\cos\theta + 3\sin\theta$ represents a straight line
- D. $\frac{l}{r} = 1 + \cos\theta$ in an ellipse

3 The pedal equation of the parabola $\frac{2a}{r} = 1 - \cos\theta$ with respect to the focus as pole, is :

~~A.~~ $p^2 = ar$

B. $r^2 = \frac{p^2}{2a}$

C. $r = p$

D. $r^2 = ap$

4 Which of the statement is TRUE?

A. A unit in a ring cannot be a zero divisor

B. A commutative ring with unit element without zero divisors is an integral domain

C. A Euclidean ring has a unit element

~~D.~~ All of these are true

5

A particle is moving in a straight line with uniform acceleration. If its velocity at any two points are u, v then its velocity at the midpoint will be -

~~A.~~ $\sqrt{\frac{(u^2 + v^2)}{2}}$

B. $\sqrt{\frac{(u^2 + v^2)}{3}}$

C. $\sqrt{2(u^2 + v^2)}$

D. $\sqrt{\frac{(u^2 \cdot v^2)}{2}}$

6

A particle is projected under gravity $g = 9.81 \text{ m/sec}^2$ with velocity 29.43 m/sec at an elevation 30° . The time of flight is :

A. 15

B. 2

C. 4

~~D.~~ 3

7

A billiard ball collides directly with another ball of same mass in rest. If "e" is coefficient of restitution, then ratio of velocities after impact -

~~A.~~ $(1 - e) : (1 + e)$

B. $(2 - e) : (2 + e)$

C. $\frac{e}{2} : \frac{2}{e}$

D. $\frac{e}{1+e} : \frac{e}{1-e}$

8

A particle moves with a uniform speed, then the acceleration of the particle is :

A. Uniform

B. Positive

C. Negative

~~D.~~ Zero

9

The moment of inertia of a thin uniform rod of length $2a$ and mass M about the line through one end of the rod of perpendicular to the rod is :

A. $\frac{M(2a)^2}{3}$

B. $\frac{2}{3}M^2a$

C. $\frac{2}{3}Ma^2$

D. $\frac{2}{3}Ma$

10

A ball falls from a height 'h' upon a fixed horizontal plane with coefficient of restitution 'e'. The whole distance covered by the ball before it comes to rest is :

A. $\frac{(1+e^2)}{(1-e^2)}h$

B. $\frac{(1-e^2)}{(1+e^2)}h$

C. $\frac{(1+e^2)}{(1-e^2)}h$

D. $\left(\frac{1-e^2}{1+e^2}\right)h$

11 A cyclist describes a circular path with velocity 21 kmph. The radius of the path so that the cyclist does not slip should be greater than :
(when μ = coefficient of friction = $25/36$)

A. 2.1

B. 3

C. 6

~~D. 5~~

12 Two particles of mass 10 kg and 15 kg are dropped from a height 10 m and 40 m respectively. The ratio of their time to reach the ground is :

~~A. 1 : 2~~

B. 2 : 1

C. 4 : 1

D. 1 : 4

13	<p>A square lamina of diagonal "l" and mass "M" has moment of inertia about its diagonal as -</p> <p>A. $\frac{Ml^2}{24}$</p> <p>B. $\frac{Ml^2}{3}$</p> <p>C. $\frac{Ml^2}{8}$</p> <p>D. $\frac{Ml^2}{2}$</p>
14	<p>The displacement equation of a particle is given by $S = a \cos \omega t + b \sin \omega t$, where a, b, ω are constants. The path is :</p> <p>A. Rectilinear</p> <p>B. Simple harmonic</p> <p>C. Elliptic</p> <p>D. Circular</p>

15 A ball of mass 2 kg impinges directly on a ball of mass 1 kg which is at rest. The velocity of the former before impact is equal to the velocity of the latter after impact. The coefficient of restitution "e" is :

- A. 1/4
- B. 1
- C. 1/2
- D. 1/3

16 A particle is projected with the velocity 49 m/sec at an elevation 30° . The greatest height attained is:
[where $g = 9.8 \text{ m/sec}^2$ gravitational force]

- A. $\frac{25g}{8}$
- B. 30g
- C. 4.9g
- D. $\frac{8g}{25}$

17

The moment of inertia of a right angled isosceles triangle about the hypotenuse of length "a" is :

~~A.~~ $\frac{Ma^2}{24}$

B. $\frac{4Ma^2}{3}$

C. $\frac{2Ma^2}{3}$

D. $\frac{M^2a}{24}$

18

The radius of curvature at the lowest point of the catenary $y = c \cosh\left(\frac{x}{c}\right)$ is

~~A.~~ c

B. 0

C. ∞

D. 1

19	<p>The evolute of the cycloid is :</p> <p>A. Another cycloid</p> <p>B. Parabola</p> <p>C. Ellipse</p> <p>D. Hyperbola</p>
20	<p>Radius of curvature for the cardioid $r = a(1 + \cos\theta)$ is :</p> <p>A. $\frac{2}{3}\sqrt{ar}$</p> <p>B. $\frac{1}{3}\sqrt{3ar}$</p> <p>C. $\frac{1}{3}\sqrt{2ar}$</p> <p>D. $\frac{2}{3}\sqrt{2ar}$</p>

21	<p>The points on the parabola $y^2 = 4x$ at which the radius of curvature is $+\sqrt{2}$, are –</p> <p>A. (1, 1) and (2, 2)</p> <p>B. (1, 2) and (1, -2)</p> <p>C. (2, 1) and (2, $2\sqrt{2}$)</p> <p>D. (3, $\sqrt{12}$) and (3, $-\sqrt{12}$)</p>
22	<p>$\frac{l}{r} = 1 + e \cos \theta$, where $e > 1$, is equation of –</p> <p>A. Ellipse</p> <p>B. Parabola</p> <p>C. Hyperbola</p> <p>D. None of these</p>
23	<p>The equation of asymptote of $x^3 + y^3 = 3axy$, is :</p> <p>A. $x + y - a = 0$</p> <p>B. $x - y + a = 0$</p> <p>C. $x + y + a = 0$</p> <p>D. $x - y - a = 0$</p>

24	<p>The l.p.p. Max $z = 3x_1 + 4x_2$ Subject to $x_1 - x_2 \leq -1$ $-x_1 + x_2 \leq 0$, $x_1, x_2 \geq 0$ has:</p> <p>A. Feasible solution B. Unique solution C. Infeasible solution D. Unbounded solution</p>
25	<p>When the basis matrix is not an identity matrix for an l.p.p, we introduce a new type of variable called the -</p> <p>A. Slack variable B. Surplus variable C. Artificial variable D. Dummy variable</p>

26	<p>In a simplex table of a l.p.p. alternative optimal solutions exist if –</p> <p>A. All basic Δ_j are zero</p> <p>B. At least one Δ_j is negative</p> <p>C. All Δ_j are zero or negative</p> <p>D. Any non basic Δ_j is also zero</p>
27	<p>$\theta = \beta$ represents the polar equation of –</p> <p>A. A constant angle</p> <p>B. Circle</p> <p>C. Conic</p> <p>D. Straight line</p>
28	<p>The polar equation of circle with centre $(4, \pi/4)$ and radius 2 is :</p> <p>A. $r^2 - 8\cos(\theta + \pi/4) + 12 = 0$</p> <p>B. $r^2 + 8\cos(\theta - \pi/4) + 12 = 0$</p> <p>C. $r^2 - 8\cos(\theta - \pi/4) + 12 = 0$</p> <p>D. $r^2 - 8\cos(\theta - \pi/4) - 12 = 0$</p>

29

What is the equation of the conic (in polar) if S (focus) is taken as pole and OX' (negative direction of the axis) is taken as initial line ?

A. $\frac{1}{r} = A\cos\theta + B\sin\theta$

B. $\frac{l}{r} = 1 + e\cos\theta$

C. $r = 2\cos\theta$

D. None of these

30

The lines $r(\cos\theta + \sin\theta) = \pm 1$ and $r(\cos\theta - \sin\theta) = \pm 1$ enclose a :

A. Square

B. Rhombus

C. Rectangle

D. Quadrilateral

31	<p>The envelope of a system of concentric ellipses with their axes along the coordinate axes and of constant area is :</p> <p>A. Parabola</p> <p>B. Ellipse</p> <p>C. Astroid</p> <p>D. Rectangular Hyperbola (RH)</p>
32	<p>The equation of the tangent to the circle $r = 10 \cos \theta$ at $\theta = \pi/4$ is:</p> <p>A. $r \sin \theta = 1$</p> <p>B. $r \sin \theta = 10$</p> <p>C. $r \sin \theta = 5$</p> <p>D. $r \sin \theta = 2$</p>
33	<p>Which pair of straight lines are parallel?</p> <p>A. $\cos \theta + \sin \theta = \frac{1}{r}$, $\cos \theta - \sin \theta = \frac{1}{r}$</p> <p>B. $\cos \theta + \sin \theta = \frac{\sqrt{2}}{r}$, $\cos \theta + \sin \theta = \frac{10\sqrt{2}}{r}$</p> <p>C. $2\cos \theta + \sin \theta = \frac{2}{r}$, $\cos \theta + 2\sin \theta = \frac{2}{r}$</p> <p>D. $2\cos \theta + \sin \theta = \frac{2}{r}$, $2\cos \theta - \sin \theta = \frac{2}{r}$</p>

34

Which is TRUE?

The equations

~~A.~~ $\frac{l}{r} = 1 - e \cos \theta$ and $\frac{l}{r} = -1 - e \cos \theta$

represent the same conic.

B. $r = 10 \cos \theta$ represents a straight line

C. $r \sin \theta = 10$ represents a circle

D. $r = 5$ represents a straight line

35

The directrix of the conic $\frac{l}{r} = 1 + e \cos \theta$

is:

~~A.~~ $\frac{l}{r} = e \cos \theta$

B. $\frac{l}{r} = -e \cos \theta$

C. $\frac{l}{r} = \sin \theta$

D. $\frac{l}{r} = -\sin \theta$

36	<p>The envelope of circles whose centres lie on the parabola $y^2=4ax$ and which passes through its vertex is :</p> <p>A. $x^3 + y^2(x + 2a) = 0$</p> <p>B. $y^3 + x^2(y + 2a) = 0$</p> <p>C. $x^3 + y^2(x - 2a) = 0$</p> <p>D. $y^3 + x^2(y - 2a) = 0$</p>
37	<p>Partial differential equation obtained by eliminating a and b from $az + b = a^2 x + y$ is :</p> <p>A. $\left(\frac{\partial z}{\partial x}\right) \cdot \left(\frac{\partial z}{\partial y}\right) = -1$</p> <p>B. $\left(\frac{\partial z}{\partial x}\right) \cdot \left(\frac{\partial z}{\partial y}\right) = 1$</p> <p>C. $\frac{\partial z}{\partial x} = \frac{\partial z}{\partial y}$</p> <p>D. $\frac{\partial z}{\partial x} = -\frac{\partial z}{\partial y}$</p>

38

General solution of

$$x^2 \frac{d^2y}{dx^2} - 3x \frac{dy}{dx} + 4y = 0 \text{ is:}$$

A. $(c_1 + c_2x)e^{2x}$

B. $c_1 \cdot e^{2x} + c_2 \cdot e^{-2x}$

~~C.~~ $(c_1 + c_2 \log x) \cdot x^2$

D. $(c_1 + c_2 \log x) \cdot \frac{1}{x^2}$

39

Particular integral of

$$(D^2 + D)y = x^2 + 2x + 4, \text{ where}$$

$$D \equiv \frac{d}{dx}, \text{ is:}$$

A. $x^2 + 4$

B. $\frac{x^3}{4} + 4x$

C. $\frac{x^2}{2} + 4$

~~D.~~ $\frac{x^3}{3} + 4x$

40

Particular integral of the differential

equation $(4D^2 - 12D + 9)y = 144e^{\frac{3x}{2}}$ where $D \equiv \frac{d}{dx}$ is :

A. $18x^2 e^{\frac{3x}{2}}$

B. $18x^2 e^{-\frac{3x}{2}}$

C. $36x^2 e^{\frac{3x}{2}}$

D. $36x^2 e^{-\frac{3x}{2}}$

41

The necessary and sufficient condition for the integrability of total differential

equation $Pdx + Qdy + Rdz = 0$ is :

A. $P\left(\frac{\partial Q}{\partial z} - \frac{\partial R}{\partial y}\right) - Q\left(\frac{\partial R}{\partial x} - \frac{\partial P}{\partial z}\right) + R\left(\frac{\partial P}{\partial y} - \frac{\partial Q}{\partial x}\right) = 0$

B. $P\left(\frac{\partial Q}{\partial z} - \frac{\partial R}{\partial y}\right) + Q\left(\frac{\partial R}{\partial x} - \frac{\partial P}{\partial z}\right) + R\left(\frac{\partial P}{\partial y} - \frac{\partial Q}{\partial x}\right) = 0$

C. $P\left(\frac{\partial Q}{\partial z} + \frac{\partial R}{\partial y}\right) - Q\left(\frac{\partial R}{\partial x} + \frac{\partial P}{\partial z}\right) - R\left(\frac{\partial P}{\partial y} + \frac{\partial Q}{\partial x}\right) = 0$

D. $P\left(\frac{\partial Q}{\partial z} + \frac{\partial R}{\partial y}\right) - Q\left(\frac{\partial Q}{\partial z} + \frac{\partial R}{\partial y}\right) + R\left(\frac{\partial P}{\partial y} + \frac{\partial Q}{\partial x}\right) = 0$

42

Solutions of the differential equation

$$\left(\frac{dy}{dx}\right)^2 - ax^3 = 0 \text{ are :}$$

~~A.~~ $5(y+c) = \pm 2a^{1/2} x^{5/2}$

B. $2(y+c) = \pm 5a^{1/2} x^{3/2}$

C. $2(x+c) = \pm 5a^{1/2} y^{5/2}$

D. $y+c = \pm \frac{5\sqrt{a}}{y^{5/2}}$

43

Laplace transform of

$$f(t) = e^{-2t} (3\cos 6t - 5\sin 6t)$$

A. $\frac{3s+24}{s^2+4s+40}$

~~B.~~ $\frac{3s-24}{s^2+4s+40}$

C. $\frac{3s+12}{s^2+2s+20}$

D. $\frac{3s-12}{s^2-4s+20}$

44

The slope at any point of a curve

$y = f(x)$ is given by $\frac{dy}{dx} = 3x^2$ and it

passes through $(-1, 1)$. The equation of the curve is :

~~A.~~ $y = x^3 + 2$

B. $y = -x^3 - 2$

C. $y = x^3$

D. $y = -x^3 + 2$

45

The order of the differential equation

$$\sqrt{1 + \left(\frac{dy}{dx}\right)^2} = \frac{d^2y}{dx^2}$$

A. $\frac{1}{2}$

~~B.~~ 2

C. 1

D. 4

46

If the first quartile is 104 and quartile deviation is 18, find the third quartile.

A. 138

B. 132

C. 140

D. 142

47

The solution to the differential equation
 $yz dx + zx dy + xy dz = 0$

~~A. $xyz = c$~~

B. $yz + xz + xy = c$

C. $x + y + z = c$

D. $x^2 + y^2 + z^2 = c$

48 The particular integral of differential equation $(D^2 + a^2)y = \cos ax$

A. $\frac{x}{2a} \cos ax$

B. $\frac{x}{2a} \sin ax$

C. $\frac{1}{2a} \sin ax$

D. $\frac{-1}{2a} \cos ax$

49 The complimentary function of $(x^2D^2 - 3xD - 5)y = 0$

A. $Ae^{5x} + Bx^{-1}$

B. $\frac{A}{x^5} + Bx$

C. $Ax^5 + \frac{B}{x}$

D. $A \cos 5x + B \sin x$

50	<p>The complimentary function of $(D^2+4)y = \sin 2x$</p> <p>A. $A \cos 2x + B \sin 2x$</p> <p>B. $Ae^{-2x} + Be^{2x}$</p> <p>C. $e^{-x}(A \sin 4x + B \sin 4x)$</p> <p>D. $e^{-2x}(A \sin 2x + B \sin 2x)$</p>
51	<p>The partial differential equation by eliminating a, b of $Z = ax^3 + by^3$ is :</p> <p>A. $px + qy = z$</p> <p>B. $px^3 + 9y^3 = z$</p> <p>C. $px + qy = 3z$</p> <p>D. $p^3x + q^3y = z$</p>
52	<p>The value of $I.(\sin 3t \cos 4t)$ is :</p> <p>A. $\frac{1}{2} \left[\frac{7}{s^2 + 49} - \frac{1}{s^2 + 1} \right]$</p> <p>B. $\frac{1}{2} \left[\frac{7}{s^2 + 49} + \frac{1}{s^2 + 1} \right]$</p> <p>C. $\frac{1}{2} \left[\frac{s}{s^2 + 7} - \frac{s}{s^2 + 1} \right]$</p> <p>D. $\frac{1}{2} \left[\frac{s}{s^2 + 49} - \frac{s}{s^2 + 1} \right]$</p>

53

The inverse Laplace of $\left(\frac{1}{s^2}\right)$ is:

A. t^2

B. $\frac{1}{t}$

~~C. t~~

D. $\frac{1}{t^2}$

54

The value of $L^{-1}\left(\frac{2s}{s^2+4}\right)$ is:

~~A. $\frac{1}{2}t \sin 2t$~~

B. $\frac{1}{4}t^2 \sin t$

C. $\frac{-1}{2}t \sin 2t$

D. $\frac{-t^2}{4} \sin t$

55

The differential equation

 $x dy - y dx = 2x^3 dx$ has the solution :

A. $x^2 + y = Cx^3$

~~B. $-x^3 + y = Cx$~~

C. $x^3 + y = Cx$

D. $-x^2 + y = C$

56

The Laplace transform $L(te^t)$ is :

~~A. $\frac{1}{(s-1)^2}$~~

B. $\frac{-1}{(s-1)^2}$

C. $\frac{1}{(s+1)^2}$

D. $\frac{1}{s^2}$

57	<p>Which of the following is NOT a general method for solving operations research models ?</p> <ul style="list-style-type: none">A. Analytic methodB. Iterative method<input checked="" type="checkbox"/> C. Probabilistic methodD. The Monte-Carlo method
58	<p>The simple method of linear programming was developed by –</p> <ul style="list-style-type: none"><input checked="" type="checkbox"/> A. George B. DantzigB. CantorC. George BooleD. Jhonson
59	<p>Which one of the following type does NOT form the part of constraints in l.p.p ?</p> <ul style="list-style-type: none">A. Less than or equal to<input checked="" type="checkbox"/> B. Not equal toC. Greater than or equal toD. Equal to

60	<p>Equation $r = a$ represents the polar equation of –</p> <p>A. Straight line</p> <p>B. Circle</p> <p>C. Cone</p> <p>D. Cylinder</p>
61	<p>The angle of intersection of the curves $r = \sin\theta + \cos\theta$ and $r = 2 \sin\theta$ is :</p> <p>A. $\frac{\pi}{4}$</p> <p>B. $\frac{3\pi}{4}$</p> <p>C. $\frac{5\pi}{4}$</p> <p>D. $\frac{7\pi}{4}$</p>
62	<p>The number of factors of the number 2025 is :</p> <p>A. 25</p> <p>B. 81</p> <p>C. 8</p> <p>D. 15</p>

63

$$\frac{1^2 \cdot 2}{1} + \frac{2^2 \cdot 3}{2} + \frac{3^2 \cdot 4}{3} + \frac{4^2 \cdot 5}{4} + \dots$$

The sum of the above series is :

A. $5e$

B. $3e$

C. $7e$

D. $2e$

64

Fermat's theorem states " If P is prime and a is any number prime to P then a^P is divisible by P". What is N ?

A. $a^{P+1} - 1$

B. $a^P - 1$

C. $a^{P-1} + 1$

D. $a^{P-1} - 1$

65

The sum of all divisors of 480 is .

A. 706

B. 1412

C. 252

D. 398

66

$$\lim_{x \rightarrow a} \left(2 - \frac{x}{a} \right)^{\tan \frac{\pi x}{2a}} =$$

A. $e^{2\pi}$

B. e^1

C. $\frac{\pi}{2}$

~~D. $e^{2/\pi}$~~

67

$$\lim_{x \rightarrow b} \frac{x^b - b^x}{x^x - b^b} = ?$$

~~A. $\frac{1 - \log b}{1 + \log b}$~~

B. $\log b$

C. $\frac{1}{\log b}$

D. $\frac{1 + \log b}{1 - \log b}$

68

The sum of the series

$$2 \left[1 + \frac{(\log e^n)^2}{2} + \frac{(\log e^n)^4}{4} + \dots \infty \right] = ?$$

A. $n^2 + 1$

B. $n + 1/n$

C. $n^2 - 1$

D. $n - 1/n$

69

If $\left| \frac{1}{2n+1} \right| < 1$ then

$$2 \left[\frac{1}{(2n+1)} + \frac{1}{3(2n+1)^3} + \frac{1}{5(2n+1)^5} + \dots \right] =$$

A. $\log\left(\frac{n}{n+1}\right)$

B. $\log\left(\frac{n+1}{n}\right)$

C. $\log\left(\frac{2n+1}{n}\right)$

D. $\log\left(\frac{n}{2n+1}\right)$

70

$$\lim_{x \rightarrow 0} \frac{e^{ax} - e^{bx}}{x} =$$

A. $e^a - e^b$

B. e^{a-b}

C. e^{b-a}

~~D. $(a - b)$~~

71

The numbers 496 is:

A. Fibonacci number

B. Fermat number

~~C. Perfect number~~

D. Prime number

72

The sum of the series using Binomial

theorem $1 + \frac{3}{4} + \frac{3.5}{4.8} + \frac{3.5.7}{4.8.12} + \dots$ is:

A. $\sqrt{2} + 1$

B. $\sqrt{2} - 1$

C. $2\sqrt{2} - 1$

~~D. $2\sqrt{2}$~~

73

The sum of the series to ∞

$$\frac{1}{\lfloor 1 \rfloor} + \frac{1+2}{\lfloor 2 \rfloor} + \frac{1+2+3}{\lfloor 3 \rfloor} + \dots + \infty \text{ is:}$$

A. $e/2$

B. e

~~C. $\frac{3}{2}e$~~

D. $2e$

74

When $|x| < 1$ and if

$$f = \frac{x}{1+x^2} + \frac{1}{3} \left(\frac{x}{1+x^2} \right)^3 + \frac{1}{5} \left(\frac{x}{1+x^2} \right)^5 + \dots$$

$$\text{then } \frac{1}{2} \log \left(\frac{1+x+x^2}{1-x+x^2} \right) = \dots$$

A. $2f$

~~B. f~~

C. f^2

D. $3f$

75

The sum of the series

$$\left(\frac{a-b}{a}\right) + \frac{1}{2}\left(\frac{a-b}{a}\right)^2 + \frac{1}{3}\left(\frac{a-b}{a}\right)^3 + \dots$$

will be equal to :

- A. $\log_e ab$
- B. $\log_e (b : a)$
- C. $\log_e (a / b)$
- D. $\log_e a^b$

76

If $Y = x - \frac{x^2}{2} + \frac{x^3}{3} - \frac{x^4}{4} + \dots \infty$

and $|x| < 1$ then

$y + \frac{y^2}{2} + \frac{y^3}{3} + \frac{y^4}{4} + \dots \infty$ is :

- A. e^x
- B. x
- C. $\log_e (1 + y)$
- D. $\log_e (1 - y)$

77	<p>The equation</p> $x^2 + y^2 + z^2 + 2ux + 2vy + 2wz + d = 0$ <p>represents a sphere iff $u^2 + v^2 + w^2 - d$ is :</p> <p>A. Zero or negative</p> <p>B. Negative</p> <p>C. Zero</p> <p><input checked="" type="checkbox"/> D. Positive</p>
78	<p>The radius of circle in which the sphere</p> $x^2 + y^2 + z^2 + 2x - 2y - 4z - 19 = 0$ <p>is cut by the plane $x + 2y + 2z + 7 = 0$ is:</p> <p>A. 4</p> <p>B. 1</p> <p>C. 2</p> <p><input checked="" type="checkbox"/> D. 3</p>

79	<p>The shortest distance from the plane $12x + 4y + 3z = 327$ to the sphere $x^2 + y^2 + z^2 + 4x - 2y - 6z = 155$ is:</p> <p>A. 39</p> <p>B. 26</p> <p>C. $41\frac{4}{13}$</p> <p>D. 13</p>
80	<p>$\int_{-\pi}^{\pi} \int_0^2 r \sin \theta dr d\theta = ?$</p> <p>A. 0</p> <p>B. π</p> <p>C. $-\pi$</p> <p>D. 2</p>
81	<p>If $y = e^{\tan^{-1} x}$ then $(1 + x^2)y_2 + 2xy_1 = ?$</p> <p>A. y</p> <p>B. y_1</p> <p>C. y^2</p> <p>D. $3y_1$</p>

82

The area bounded by one arch of the cycloid

$$x = a(\theta - \sin \theta)$$

$$y = a(1 - \cos \theta)$$

and the x-axis is:

~~A.~~ $3\pi a^2$

B. $4\pi a^2$

C. πa^2

D. $2\pi a^2$

83

The value of $\sqrt{(1/2)}$ is:

A. $\pi/2$

B. $-2\sqrt{\pi}$

C. π

~~D.~~ $\sqrt{\pi}$

84

If $I_n = \int_0^{\frac{\pi}{2}} \tan^n x dx$ then $I_n + I_{n-2} =$

A. $\frac{1}{n-2}$

B. $\frac{1}{n}$

C. $\frac{n}{n-1}$

~~D. $\frac{1}{n-1}$~~

85

$\int_{-1}^2 |x-1| dx =$

A. $2/5$

B. 5

~~C. $5/2$~~

D. 2

86

If $y = \sin^{-1} x$ then $(1 - x^2)y_2 =$

A. xy

B. y_1

~~C. xy_1~~

D. x^2y

87

$$\int_0^x \sqrt{x} e^{-x^3} dx =$$

A. $\sqrt{\pi}$

~~B. $\sqrt{\pi}/3$~~

C. $\sqrt{\pi}/2$

D. $\pi/3$

88

$$\int_0^{\pi/6} \sin^{-3} 3x \, dx =$$

A. $\frac{8}{15}$

B. 105

C. 48

~~D. $\frac{16}{105}$~~

89

If $x+y+z = u$, $y+z = uv$, $z = uvw$ then

$$\frac{\partial(x, y, z)}{\partial(u, v, w)} = ?$$

A. u^2

~~B. u^2v~~

C. uvw

D. uv^2

90

$$\int e^x (\tan x + \sec^2 x) dx =$$

A. $e^x \tan x \sec x + c$

B. $e^x \tan x + c$

C. $e^x \sec^2 x + c$

D. $e^2 \sec x + c$

91

Evaluate $\iint_R y^2 dx dy$ when R is the region bounded by $y = 2x$, $y = 5x$ and $x = 1$.

A. 117

B. 39

C. 48

D. $\frac{39}{4}$

92

$$\int_0^x \frac{dx}{(1+x^2)^2} =$$

A. $\pi/4$

B. $\pi/8$

C. π

D. 2π

93

If $x = u(1+v)$ and $y = v(1+u)$ then

$$\frac{\partial(x,y)}{\partial(u,v)} = ?$$

A. $u+v$

B. $1+u$

C. $1+u+v$

D. $1+v$

94

In which of the following cases

$$(1-x^2)y_2 - xy_1 = 0 \text{ where } y_1 = \frac{dy}{dx} \text{ and}$$

$$y_2 = \frac{d^2y}{dx^2}$$

A. $\text{Cos}(m \sin^{-1} x) = y$

B. $y = (\sin^{-1} x)^2$

~~C.~~ $y = (\cos^{-1} x)$

D. $y = \tan^{-1} x$

95

$$\int_0^{\pi/2} \int_0^{\pi/2} \sin(\theta + \phi) d\theta d\phi = ?$$

A. 1

B. 0

C. 3

~~D.~~ 2

96

$\{0, 1\}$ is a set with the operations defined by the following tables :

+	0	1
0	0	1
1	1	0

.	0	1
0	0	0
1	0	1

Which statement is TRUE?

- A. $\{0, 1\}$ is not a ring
- B. $\{0, 1\}$ is a ring
- C. $\{0, 1\}$ is a ring with unit element
- D. $\{0, 1\}$ is a commutative ring with unit element

97

If T is an automorphism of a group G such that $Tx = x^{-1} \forall x \in G$, then:

- A. G is not abelian
- B. G is abelian
- C. $\text{Ker } T \neq \{e\}$
- D. T^{-1} does not exist

98

The order of 2 and 3 in $(Z_8, +_8)$ are:

- A. $O(2) = 4$. $O(3) = 8$
- B. $O(2) = 2$. $O(3) = 4$
- C. $O(2) = 8$, $O(3)$ is infinite
- D. $O(2) = 0$. $O(3) = 1$

99

Consider the group $G = \{1, -1, i, -i\}$ under multiplication. Then-

- A. G is a cyclic group generated by 1
- B. G is a cyclic group generated by -1
- C. G is a cyclic group generated by i only
- D. G is a cyclic group generated by i and - i

100

The product of two eigen values of

$$A = \begin{bmatrix} 6 & -2 & +2 \\ -3 & 3 & -1 \\ 2 & -1 & 3 \end{bmatrix}$$

is 14. Find the

A. 1

B. 2

C. 3

D. 4

101

Rank of $\begin{bmatrix} 9 & 7 & 3 \\ 5 & -1 & 4 \\ 3 & 5 & 1 \end{bmatrix}$ = rank of

$$\begin{bmatrix} 9 & 7 & 3 & 6 \\ 5 & -1 & 4 & 1 \\ 3 & 5 & 1 & 2 \end{bmatrix} = 3$$

then the system of equations:

$$9x - 7y + 3z = 6$$

$$5x - y - 4z = 1$$

$$3x + 5y + z = 2$$

A. Are consistent and posses infinite number of solutions

B. Are consistent and posses unique solution

C. Are inconsistent and posses no solution

D. Have solutions other than (1, 0, -1)

102

The inverse of $A = \begin{bmatrix} 2 & 3 \\ 4 & 5 \end{bmatrix}$ is:

~~A.~~ $\begin{bmatrix} -5/2 & 3/2 \\ 2 & -1 \end{bmatrix}$

B. $\begin{bmatrix} 5/2 & 3/2 \\ -2 & 1 \end{bmatrix}$

C. $\begin{bmatrix} -5 & 3 \\ 1 & -1/2 \end{bmatrix}$

D. does not exist

103

The eigen values of $A = \begin{bmatrix} 3 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 3 \end{bmatrix}$

are

A. -1, 3, -4

~~B.~~ 1, 3, 4

C. 3, 3, 2

D. 1, 5, 2

104

If R is a ring with zero element, then which is TRUE?

- A. $\{0\}$ is an ideal in R but R is not ideal in R
- B. R is an ideal but $\{0\}$ is not an ideal in R
- C. Both $\{0\}$ and R are ideals in R
- D. R has no non trivial ideals or improper ideals

105

Which of the following is true?

- A. The ring Z of integers has a zero divisor
- B. The ring Q of rationals has a zero divisor
- C. The ring r of reals has a zero divisor
- D. Z, Q, R and C have no divisors of zero

106	<p>Q = The set of rationals, under usual multiplication is:</p> <p>A. A group</p> <p>B. Not a group</p> <p>C. A commutative group</p> <p>D. Not closed</p>
107	<p>Let G is a group of prime order P. Then which is false?</p> <p>A. G is cyclic</p> <p>B. G has no proper sub groups</p> <p>C. G has proper sub groups</p> <p>D. G has P-1 generators</p>
108	<p>If G is a group, then the centre Z (G) is defined by $Z(G) = \{z \in G / z x = x z \text{ for all } x \in G\}$. Then-</p> <p>A. Z (G) is not a sub group of G</p> <p>B. Z (G) is a sub group of G but not normal</p> <p>C. Z (G) is a normal sub group of G</p> <p>D. $G = Z (G)$</p>

109 Let H and K be two finite sub groups of a group G . Then which of the following is NOT true?

- A. HK is not a sub group of G if $HK = KH$
- B. HK is a sub group of G if and only if $HK = KH$
- C. HK is a sub group of G if G is abelian
- D. $O(HK) = \frac{O(H) O(K)}{O(H \cap K)}$

110 Let $G = \{1, -1, i, -i\}$, which is normal?

- A. $\{-1, i\}$
- B. $\{-1, -i\}$
- C. $\{1, -1\}$
- D. $\{i, -i\}$

- 111 Let G is a group of order 2 then -
- A. There is no automorphism of G
 - B. There can be many automorphism of G
 - C. There is only one automorphism that is the identity mapping
 - D. There is only one automorphism that is not the identity mapping

- 112 A person goes from x to y on cycle at 20 km/hr & returns at 24 km/hr. His average speed is:
- A. 22
 - B. 21.82
 - C. 22.42
 - D. 23.12

113 Find the value of p for the following distribution whose mean is 16.6.

x: 8 12 15 p 20 25 30
f: 12 16 20 24 16 8 4

A. 16.5

B. 17.5

C. 16

~~D. 18~~

114 Karl - Pearson's Coefficient of skewness is given by, Skewness =

A. $\frac{\text{Mode-Mean}}{\text{Standard Deviation}}$

B. $\frac{\text{Standard deviation}}{\text{Mean-Mode}}$

~~C. $\frac{\text{Mean-Mode}}{\text{Standard deviation}}$~~

D. $\frac{\text{Standard deviation}}{\text{Mode-Mean}}$

115 Bowley coefficient of skewness lies between:

A. -1 and +1

B. -3 and +3

C. -0.5 and 0.5

D. None of these

116 Coefficient of Correlation is the _____ mean of regression coefficients.

A. Arithmetic

B. Geometric

C. Harmonic

D. Grouped mean

117 Moment generating function of a normal random variable about its origin is given by :

A. $e^{-ut + \frac{1}{2}\sigma^2 t^2}$

B. $e^{ut - \frac{1}{2}\sigma^2 t^2}$

C. $e^{\mu - \frac{1}{2}\sigma^2 t^2}$

D. $e^{-[ut - \frac{1}{2}\sigma^2 t^2]}$

- 118 Arithmetic mean of two regression coefficients is:
- A. Square root of the correlation coefficient
 - B. Equal to the correlation coefficient
 - C. Less than the correlation coefficient
 - D. Greater than the correlation coefficient

- 119 The odds that x speaks the truth are 3:2 and the odds that person y speaks truth are 3:5. In what percentage of cases are they likely to contradict each other on an identical point?
- A. 45.5%
 - B. 46.5%
 - C. 47.5%
 - D. 47.8%

120 In a binomial distribution, which of the following is wrong?

A. Mean = np

B. $0 < p < 1$. $0 < q < 1$

~~C. Mean \leq Variance~~

D. Variance = npq

121 In a normal distribution, ratio between Quartile deviation, Mean deviation & Standard deviation is:

~~A. 10 : 12 : 15~~

B. 10 : 11 : 15

C. 10 : 14 : 15

D. 11 : 13 : 15

122 Which of the following statement is FALSE?

- A. Two independent variables are uncorrelated
- B. $r(x, y)=0 \Rightarrow$ Absence of any linear relationship between x and y
- ~~C. Uncorrelated variables are independent~~
- D. Correlation coefficient is independent of change of origin and scale

123 χ^2 - distribution CANNOT be applied to test:

- A. If the hypothetical value of the population variance is $\sigma^2 = \sigma_0^2$ (say)
- B. The goodness of fit
- C. The independence of attributes
- ~~D. If the hypothetical value of the population mean is $\bar{x} = \mu$ (say)~~

124 99 % fiducial limits for the mean of normal distribution are :

A. $\bar{x} \pm 2.58 \frac{\sigma}{n}$

B. $\bar{x} \pm 2.58 \frac{\sigma}{\sqrt{n-1}}$

C. $\bar{x} \pm 2.58 \frac{\sigma}{\sqrt{n}}$

D. $\bar{x} \pm 2.33 \frac{\sigma}{\sqrt{n-1}}$

125 Coefficient skewness of a Poisson distribution is:

A. $1/\lambda$

B. $3 + \frac{1}{\lambda}$

C. $1 - \lambda$

D. $\lambda - 1$

126

χ^2 - Values _____ with the _____
in degrees of freedom.

- A. Increase, Decrease
- B. Decrease, Increase
- C. Increase, Increase
- D. Remain constant, Increase

127

A & B are events such that

$$p(A \cup B) = \frac{3}{4}, p(A \cap B) = \frac{1}{4}$$

$$P(\bar{A}) = \frac{2}{3} \text{ then } P(B) = ?$$

- A. $\frac{2}{3}$
- B. $\frac{1}{3}$
- C. $\frac{1}{12}$
- D. $\frac{3}{4}$

128

Given two regression lines:

$$3x + 2y = 26 \text{ and}$$

$$6x + y = 31$$

Find the regression coefficient by x .

A. $\frac{3}{2}$

B. $\frac{-3}{2}$

C. $\frac{-1}{6}$

D. $\frac{1}{6}$

129

Compute the quartiles Q_1 , Q_2 , and Q_3 for
the data :

9, 13, 14, 7, 12, 17, 8, 10, 6, 15, 18, 21, 20

A. 8, 13, 17

B. 8.5, 13, 17.5

C. 8, 13.5, 17.5

D. 8.5, 13.5, 17.5

130	<p>The best measure of comparing the variability of two series is:</p> <p>A. Standard deviation</p> <p><input checked="" type="checkbox"/> B. Coefficient of variation</p> <p>C. Correlation coefficient</p> <p>D. Coefficient of skewness</p>
131	<p>In testing the independence of attributes in a 3 x 3 contingency table, using χ^2-test, the number of degrees of freedom is:</p> <p><input checked="" type="checkbox"/> A. 4</p> <p>B. 8</p> <p>C. 6</p> <p>D. 12</p>
132	<p>If $\phi = \log r$ then $\nabla \phi$ is :</p> <p>A. $-\vec{r}/r^2$</p> <p><input checked="" type="checkbox"/> B. $+\vec{r}/r^2$</p> <p>C. $-\vec{r}/r^3$</p> <p>D. $+\vec{r}/r^3$</p>

133 The side of a square lamina ABCD is $2a$ metres. Along \overline{AB} , \overline{CB} , \overline{CD} , \overline{AD} and \overline{BD} act forces of magnitudes 1, 2, 3, 4 and 5 kg weight respectively. Then the algebraic sum of their moments about the centre of the square is:

- A. $-2a$ kg metres
- B. $-2\sqrt{2}a$ kg metres
- C. $(2 + 5\sqrt{2})a$ kg metres
- D. $(2 - 5\sqrt{2})a$ kg metres

134 Two equal unlike parallel forces form a -

- A. Resultant force
- B. Coplanar system
- C. Couple
- D. Parallel system

135 Three forces acting on a particle are in equilibrium. The angle between the first and the second is 90° and that between the second and the third is 120° . The ratio of the forces is:

~~A.~~ $\sqrt{3} : 1 : 2$

B. $1 : 2 : \sqrt{3}$

C. $1 : \sqrt{3} : 2$

D. $\sqrt{3} : 2 : 1$

136 The resultant of two forces P and Q is R_1 . If one of the forces be reversed in direction, the resultant becomes R_2 .

Then $R_1^2 + R_2^2$ is:

A. $R_1^2 + R_2^2 = 0$

B. $R_1^2 + R_2^2 = P^2$

~~C.~~ $R_1^2 + R_2^2 = 2(P^2 + Q^2)$

D. $R_1^2 + R_2^2 = 2(P^2 - Q^2)$

137

The centre of gravity of a solid cone of height h lies on the axis at a distance of:

A. $\frac{3}{8}h$ from the vertex

B. $\frac{h}{3}$ from the vertex

C. $\frac{3h}{4}$ from the vertex

D. $\frac{h}{2}$ from the vertex

138

Two forces \overline{P} and \overline{Q} act on a particle. If the sum and difference of forces are at right angles to each other, then:

A. $P > Q$

B. $Q > P$

C. $P = Q$

D. $P \neq Q$

139 Two forces of magnitudes P and Q act at a point. If the direction of \vec{Q} is reversed, then the resultant turns through a right angle. Then:

A. $P = 2Q$

B. $Q = 2P$

C. $P = Q$

D. $P \neq Q$

140 S is the circum centre of a triangle ABC . If forces of magnitudes $\vec{P}, \vec{Q}, \vec{R}$ acting along SA, SB, SC are in equilibrium, then:

A. $\frac{P}{\sin A} = \frac{Q}{\sin B} = \frac{R}{\sin C}$

B. $\frac{P}{\sin A/2} = \frac{Q}{\sin B/2} = \frac{R}{\sin C/2}$

C. $\frac{P}{\sin 2A} = \frac{Q}{\sin 2B} = \frac{R}{\sin 2C}$

D. $\frac{P}{\cos A} = \frac{Q}{\cos B} = \frac{R}{\cos C}$

141 If λ is the angle of friction, then $\tan \lambda = \mu$ is :

- A. $\frac{\text{Limiting friction}}{\text{Normal reaction}}$
- B. $\frac{\text{Force of friction}}{\text{Reaction}}$
- C. $\frac{\text{Normal reaction}}{\text{Reaction}}$
- D. $\frac{\text{Normal reaction}}{\text{Limiting friction}}$

142 If three parallel forces \bar{P} , \bar{Q} and \bar{R} acting at A, B and C respectively are in equilibrium, then $P : Q : R$ is :

- A. $1 : 1 : 2$
- B. $AC : CB : AB$
- C. $BC : CA : AB$
- D. $AB : BC : AC$

143

Unit normal to the surface $x^2y + 2xz = 4$ at the point $(2, -2, 3)$ is :

A. $\frac{\hat{i} + 2\hat{j} + 2\hat{k}}{3}$

B. $\frac{\hat{i} - 2\hat{j} + 2\hat{k}}{3}$

C. $\frac{\hat{i} + 2\hat{j} - 2\hat{k}}{3}$

~~D. $\frac{-\hat{i} + 2\hat{j} + 2\hat{k}}{3}$~~

144

I is the in centre of a triangle ABC. If forces \vec{P} , \vec{Q} , \vec{R} acting along IA, IB, IC are in equilibrium, then-

A. $\frac{P}{\cos A} = \frac{Q}{\cos B} = \frac{R}{\cos C}$

B. $\frac{P}{\cos \frac{A}{2}} = \frac{Q}{\cos \frac{B}{2}} = \frac{R}{\cos \frac{C}{2}}$

C. $\frac{P}{\cos 2A} = \frac{Q}{\cos 2B} = \frac{R}{\cos 2C}$

D. $\frac{P}{\sin \frac{A}{2}} = \frac{Q}{\sin \frac{B}{2}} = \frac{R}{\sin \frac{C}{2}}$

145

$$\vec{V} \times \vec{r} =$$

A. A constant vector

B. Zero vector

C. $\frac{\vec{r}}{|\vec{r}|}$

D. None of these

146

$\int_C (xy - x^2) dx + x^2 y dy$ over the triangle

bounded by the lines $y = 0$, $x = 1$, $y = x$ is :

A. $\frac{1}{12}$

~~B. $-\frac{1}{12}$~~

C. $\frac{1}{24}$

D. $-\frac{1}{24}$

147

If $t_n = \frac{\sum^n n}{n}$ then $\sum_{n=0}^x t_n = ?$

A. e

B. e^{-1}

~~C. $\frac{3e}{2}$~~

D. $\frac{e}{2}$

148

If $\vec{F} = x\hat{i} + y\hat{j} + z\hat{k}$ and S is taken over the region bounded by the planes $x = 0$, $x = a$, $y = 0$, $y = a$, $z = 0$ and $z = a$, then

the value of $\int_S \vec{F} \cdot \hat{n} ds$ is:

- A. a^3
~~B. $3a^3$~~
 C. $\frac{a^3}{3}$
 D. $4a^3$

149

If $\vec{r} = x\hat{i} + y\hat{j} + z\hat{k}$ is the position vector of the point (x, y, z) then the value of

$\nabla^2 \left(\frac{1}{r} \right)$ is:

- A. $-\frac{\vec{r}}{r^3}$
~~B. 0~~
 C. 3
 D. $\frac{1}{3}$

150

If \vec{A} and \vec{B} are irrotational, which of the following is WRONG?

A. $\vec{B} \cdot (\nabla \times \vec{A}) = 0$

B. $\vec{A} \cdot (\nabla \times \vec{B}) = 0$

C. $\vec{A} \times \vec{B}$ is not solenoidal

D. $\vec{A} \times \vec{B}$ is solenoidal

151

If \vec{r} is the position vector of the point (x, y, z) then which is TRUE?

A. $\text{div } \vec{r} = 3$

B. $\nabla \vec{r} = \frac{\vec{r}}{r}$

C. $\nabla \times \vec{r} = 0$

D. All of these are true

152

Unit vector normal to the surface

$$x^2 + 3y^2 + 2z^2 = 6$$
 at the point

(2, 0, 1) is:

A.
$$\frac{\hat{i} + 2\hat{k}}{\sqrt{5}}$$

~~B.
$$\frac{\hat{i} + \hat{k}}{\sqrt{2}}$$~~

C.
$$\frac{\hat{i} + \hat{j} + \hat{k}}{3}$$

D.
$$\frac{\hat{i} + 2\hat{j} + 3\hat{k}}{\sqrt{14}}$$

153

The directional derivative of xyz at the

point (1, 2, -1) in the direction of

$$\hat{i} - \hat{j} - 3\hat{k}$$
 is:

A.
$$\frac{7}{\sqrt{11}}$$

~~B.
$$-\frac{7}{\sqrt{11}}$$~~

C.
$$\frac{29}{\sqrt{11}}$$

D.
$$-\frac{29}{\sqrt{11}}$$

154	<p>If a system of coplanar forces reduces neither to a single force nor to a single couple, then the system is :</p> <p>A. Diverging one B. In equilibrium C. Not in equilibrium D. None of these</p>
155	<p>Symmetric difference of sets A and B is defined as:</p> <p>A. $(A - B) \cap (B - A)$ B. $(A - B) \cup (B - A)$ C. $(A - B) \cap (B + A)$ D. $(A + B) \cup (B - A)$</p>
156	<p>A closed subspace of a compact metric space is :</p> <p>A. Open B. Compact C. Need not be compact D. None of these</p>

157	<p>In a metric space M, the full space M is :</p> <p>A. An open set</p> <p>B. A closed set</p> <p>C. Neither open nor closed</p> <p><input checked="" type="checkbox"/> D. Both open and closed</p>
158	<p>Which of the following is compact?</p> <p>A. Set of all integers in \mathbb{R}'</p> <p>B. Set of all rationals in \mathbb{R}'</p> <p><input checked="" type="checkbox"/> C. $[1,2]$ in \mathbb{R}'</p> <p>D. $(0,\infty)$ in \mathbb{R}'</p>
159	<p>For the sequence</p> $\{a_n\}_{n=1}^{\infty} = \{(-1)^n\}_{n=1}^{\infty}$ <p>$\limsup_{n \rightarrow \infty} a_n = ?$</p> <p>A. 0</p> <p>B. -1</p> <p><input checked="" type="checkbox"/> C. 1</p> <p>D. None of these</p>

160	<p>Which of the following set is NOT “nowhere dense” in \mathbb{R}^1 ?</p> <p>A. The set of all positive integers</p> <p>B. The Cantor set</p> <p>C. Every finite subset of \mathbb{R}^1</p> <p><input checked="" type="checkbox"/> D. The interval $(0,1)$ in \mathbb{R}^1</p>
161	<p>If $M = \mathbb{R}_d$, the real line with discrete metric, and if ‘a’ is any point in \mathbb{R}_d then</p> <p>1) $B[a,1]= ?$ and</p> <p>2) $B[a,2]= ?$</p> <p>A. $(a-1, a+1), (a-2, a+2)$</p> <p>B. $\{a\}, \{a\}$</p> <p><input checked="" type="checkbox"/> C. $\{a\}, \mathbb{R}_d$</p> <p>D. $\{a\}, \{a, a+1\}$</p>
162	<p>Pick the ODD man out from the following.</p> <p>A. Comparison test</p> <p>B. Cauchy’s Root test</p> <p>C. D’Alembert’s ratio test</p> <p><input checked="" type="checkbox"/> D. Leibnitz test</p>

163

The alternating series

$$\frac{1}{\sqrt{2}+1} - \frac{1}{\sqrt{3}+1} - \frac{1}{\sqrt{4}-1} - \frac{1}{\sqrt{5}+1} + \dots \text{ is:}$$

- A. Convergent
- B. Absolutely convergent
- C. Conditionally convergent
- D. Divergent

164

The series $\sum_{n=1}^x \frac{1}{(\log n)^{\log n}}$

- A. Converges
- B. Diverges
- C. May or may not converge
- D. Oscillates

165

The geometric series

$1 + x + x^2 + \dots + x^{n-1} + \dots$ is
convergent when -

- A. $0 \leq x \leq 1$
- B. $x > 1$
- C. $-1 < x < +1$
- D. $x = 1$

166	<p>Distance between any two distinct real numbers under discrete metric is :</p> <p>A. Unbounded</p> <p>B. Bounded above only</p> <p>C. Bounded below only</p> <p><input checked="" type="checkbox"/> D. Bounded</p>
167	<p>Choose the WRONG statement:</p> <p>A. A sequence has unique limit in \mathbb{R}</p> <p>B. The sequence $\{n\}_{n=1}^{\infty}$ diverges to infinity</p> <p><input checked="" type="checkbox"/> C. Every convergent sequence is unbounded</p> <p>D. None of these</p>
168	<p>The following is the n^{th} term of a sequence</p> $\frac{1}{n} + \frac{1}{n+1} + \frac{1}{n+2} + \dots + \frac{1}{2n-1}$ <p>Then the sequence is :</p> <p>A. Monotonically increasing</p> <p><input checked="" type="checkbox"/> B. Monotonically decreasing</p> <p>C. Neither increasing nor decreasing</p> <p>D. None of these</p>

169

If f and g are real valued function then $\max(f, g)$ is :

A. $\frac{|f - g| + f + g}{2}$

B. $\frac{-|f - g| + f + g}{2}$

C. $\frac{|f + g| + f + g}{2}$

D. $\frac{|f + g| + f - g}{2}$

170

Which of the following statements is NOT true?

A. The set of rationals is dense in \mathbb{R}

B. $\left\{1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}, \dots\right\}$ is not dense in $[0, 1]$

C. The discrete metric space \mathbb{R}_d has no proper dense subset

D. \mathbb{Z} – the set of integers dense in \mathbb{R} .

171

$$\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n+1} \right)^n = ?$$

A. $e + 1$ B. e C. $\frac{1}{e}$ D. $e - 1$

172

If $d = d(x, y)$ is a metric on M ,
which of the following is NOT true?

A. $\sqrt{d(x, y)}$ is also a metric on M B. $\frac{d(x, y)}{1 + d(x, y)}$ is also a metric on M C. $d^2(x, y)$ is also a metric on M D. $\min \{1, d(x, y)\}$ is also a metric on M

173

Limit point of the set

$$\left\{1, \frac{1}{2}, \frac{1}{3}, \dots, \frac{1}{n}, \dots\right\}$$

A. 1

B. $\frac{1}{2}$ ~~C. 0~~D. ∞

174

If $\lim_{n \rightarrow \infty} x_n = l$, then $\lim_{n \rightarrow \infty} \frac{x_1 + x_2 + \dots + x_n}{n}$ is equal to:~~A. l~~ B. n/l C. $\frac{l}{2}$ D. $2l$

175	<p>The coordinates of the point on the parabola $y = x^2 + 7x + 2$, which is nearest to the straight line $y = 3x - 3$ are :</p> <p>A. (-2, -8)</p> <p>B. (1, 10)</p> <p>C. (2, 20)</p> <p>D. (-1, -4)</p>
176	<p>The value of $\frac{du}{dt}$, given $u = x^2 y^3$, $x = 2t^3$, $y = 3t^2$ is :</p> <p>A. $1926 t^{11}$</p> <p>B. $30 t^{15}$</p> <p>C. $1296 t^{11}$</p> <p>D. $1692t^{11}$</p>

177 The derivative of the function

$y = \log_a x^2$ is :

A. $\frac{2}{x}$

B. $\frac{1}{x^2}$

C. $\frac{2}{x} \log_a e$

D. $\frac{1}{x^2} \log_a e$

178 $\int_0^1 x^3(1-x)^3 dx = ?$:

A. $\frac{1}{140}$

B. $\frac{\pi}{140}$

C. $\frac{\pi}{70}$

D. $\frac{1}{70}$

179 The coefficient of $(x-1)^3$ in the expansion of e^x is :

A. $\frac{e}{2}$

B. $\frac{e}{3}$

~~C. $\frac{e}{6}$~~

D. $\frac{e^3}{6}$

180 State which is FALSE:

A. For $n > 3$, the integers $n, n+2, n+4$ cannot be all primes

B. $\text{GCD}(a, a+2) = 1$ or 2 for every integer a

~~C. $2^{3n} - 1$ is not divisible by 7 for every $n \in \mathbb{N}$~~

D. $n^5 - n$ is divisible by 30 for all $n \in \mathbb{N}$

181	<p>The sum of the cubes of any three consecutive natural numbers will always be divisible by –</p> <p>A. 6</p> <p>B. 9</p> <p>C. 18</p> <p>D. More than one of these</p>
182	<p>The vectors $\alpha_1 = (6, 2, 3, 4)$, $\alpha_2 = (0, 5, -3, 1)$, $\alpha_3 = (0, 0, 7, -2)$ are:</p> <p>A. Dependent</p> <p>B. Independent</p> <p>C. Data not sufficient</p> <p>D. None of these</p>
183	<p>An example of a perfect number is :</p> <p>A. 8</p> <p>B. 30</p> <p>C. 28</p> <p>D. 48</p>

184

The coefficient of x^n in the expansion

$$1 - \frac{a+bx}{\underline{1}} + \frac{(a+bx)^2}{\underline{2}} + \frac{(a-bx)^3}{\underline{3}} + \dots \text{ is:}$$

A. $\frac{a^n n^b}{\underline{n}}$

B. $\frac{e^b a^n}{\underline{n}}$

C. $\frac{e^a n^b}{\underline{n}}$

~~D.~~ $\frac{e^a b^n}{\underline{n}}$

185

If e_1 is the eccentricity of the conic

$$9x^2 + 4y^2 = 36 \text{ and } e_2 \text{ is the eccentricity}$$

of the conic $9x^2 - 4y^2 = 36$, then -

A. $e_1^2 + e_2^2 = 2$

~~B.~~ $3 < e_1^2 + e_2^2 < 4$

C. $e_1^2 + e_2^2 > 4$

D. None of these

186 If the sum of the slopes of the lines given by $x^2 - 2cxy - 7y^2 = 0$ is 4 times their product, then c has the value -

A. -2

B. -1

~~C. 2~~

D. 1

187 The equation of a straight line joining the feet of the perpendicular from the point $(1, 0)$ on the pair of straight lines $2x^2 - 3xy + y^2 = 0$ is :

A. $3x + y + 1 = 0$

B. $2x + 3y - 1 = 0$

~~C. $x - 3y + 1 = 0$~~

D. None of these

188	<p>The radical axis of two circles is :</p> <ul style="list-style-type: none">A. Parallel to the line joining their centresB. Perpendicular to the line joining their centresC. Inclined at an angle 30° to the line joining their centresD. None of these
189	<p>The number of circles of a given radius which touch both the axes is :</p> <ul style="list-style-type: none">A. 1B. 2C. 3D. 4
190	<p>The polar of focus of a parabola is :</p> <ul style="list-style-type: none">A. x-axisB. y-axisC. DirectrixD. Latus rectum

191

A point is such that ratio of its distance from a fixed point and line $x = \frac{9}{2}$ is always 2 : 3, then the locus of the point will be -

- A. Hyperbola
- B. Ellipse
- C. Parabola
- D. Circle

192

The equation to the pair of straight lines through the origin which are perpendicular to the lines $2x^2 - 5xy + y^2 = 0$ is :

- A. $2x^2 + 5xy + y^2 = 0$
- B. $x^2 + 2y^2 + 5xy = 0$
- C. $x^2 - 5xy + 2y^2 = 0$
- D. $2x^2 + y^2 - 5xy = 0$

193

The focus of the parabola whose vertex is $(3, 2)$ and whose directrix is $x - y + 1 = 0$ is :

- A. $(4, 1)$
- B. $(1, -1)$
- C. $(8, 7)$
- D. $(-4, 1)$

194

If the line $y = 2x + c$ be a tangent to the ellipse $\frac{x^2}{8} + \frac{y^2}{4} = 1$, then $c = ?$

- A. ± 4
- B. ± 6
- C. ± 1
- D. ± 8

195

The vertex of the cone $9x^2 + 9y^2 - 4z^2 + 12yz - 6zx + 54z - 81 = 0$ is

- A. $(1, 1, 0)$
- B. $(0, 0, 0)$
- C. $(1, -2, 3)$
- D. $(1, 2, 3)$

196

The pair of straight lines $4x^2 + 6xy - y^2 = 0$ is equally inclined to the pair of straight lines :

A. $2x^2 + 2xy + y^2 = 0$

B. $5x^2 - 6xy + y^2 = 0$

C. $x^2 + 3xy + 2y^2 = 0$

D. None of these

197

The plane $x + y + z = 1$ meets the coordinate axes in A, B, C. Then the equation to the cone generated by the lines drawn from origin to meet the circle ABC is :

A. $yz + zx + xy = 0$

B. $yz + 2zx + xy = 0$

C. $yz - zx + 2xy = 0$

D. None of these

198

If 'a' and 'c' are the segments of a focal chord of a parabola and 'b' the semi-latus rectum, then -

A. a, b, c are in A.P

B. a, b, c are in G.P

~~C.~~ a, b, c are in H.P

D. None of these

199

The limiting points of the coaxial system of circles determined by

$$x^2 + y^2 - 6x - 4y + 3 = 0 \text{ and}$$

$$x^2 + y^2 + 10x + 4y - 1 = 0 \text{ are -}$$

A. (1,1) and (1,2)

~~B.~~ (+1,1) and (-1,0)

C. (2,1) and (0,1)

D. (1,-1) and (1,0)

200

Equation of a circle through origin and belonging to the co-axial system of which the limiting points are $(1,2)$, $(4,3)$ is :

A. $x^2 + y^2 - 2x + 4y = 0$

B. $x^2 + y^2 - 8x - 6y = 0$

C. $2x^2 + 2y^2 - x - 7y = 0$

D. $x^2 + y^2 - 6x - 10y = 0$